

## Post-16 Curriculum - Further Maths

### Subject Curriculum Overview

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|-------------------------------|-----------------------------------------------------|
| Subject                       | Further Maths                                       |
| Qualification / Specification | A Level Further Mathematics 7367                    |
| Awarding Body                 | AQA                                                 |
| Level                         | 3                                                   |
| Curriculum Lead               | Kamelia Howells                                     |
| Teaching Staff                | Conal Howells, Elizabeth Berrimann, Catherine Jones |
| Guided Learning Hours         | 360                                                 |
| Year(s) Delivered             | 12 & 13                                             |
| Last Review Date              | June 2026                                           |
| Next Review Date              | June 2027                                           |

### 1. Curriculum Intent

A Level Further Mathematics is designed to extend and deepen learners' understanding of mathematics beyond the standard A Level course. It provides opportunities for highly motivated and mathematically able students to explore more advanced concepts, develop sophisticated problem-solving skills, and gain a deeper appreciation of the structure, beauty, and applications of mathematics.

The subject encourages learners to think critically, reason rigorously, and approach complex problems with confidence and creativity. Through the study of advanced pure mathematics and optional content such as mechanics, statistics, decision mathematics, or further pure mathematics, learners develop a greater understanding of mathematical theory and its applications in academic, scientific, technological, and industrial contexts.

Further Mathematics provides excellent preparation for higher education, particularly for mathematically demanding courses. It enables learners to develop the depth of knowledge and analytical skills required for success in advanced study and competitive university applications.

The curriculum supports progression to degree programmes including:

- Mathematics
- Engineering
- Physics
- Computer Science
- Economics
- Data Science
- Actuarial Science
- Finance and Investment
- Operational Research
- Artificial Intelligence
- Natural Sciences

Many leading universities highly value or recommend Further Mathematics for applicants to mathematics-intensive courses because it introduces learners to concepts and methods they will encounter during the first year of undergraduate study. The subject also supports progression into higher and degree apprenticeships, particularly in STEM, technology, finance, and engineering sectors where advanced quantitative skills are essential.

Universities and employers increasingly seek individuals who can analyse complex information, solve unfamiliar problems, and think logically under pressure. Further Mathematics develops these capabilities at an advanced level.

The curriculum equips learners with:

- Advanced analytical and critical-thinking skills
- High-level problem-solving and mathematical reasoning
- The ability to model complex systems and situations
- Strong quantitative and data-handling capabilities
- Precision, accuracy, and attention to detail
- Resilience and perseverance when tackling challenging tasks
- The ability to communicate sophisticated mathematical ideas effectively

These skills are highly valued across sectors including engineering, finance, technology, data science, research, cybersecurity, artificial intelligence, and scientific innovation. The curriculum reflects the increasing demand for advanced mathematical expertise in a data-driven and technologically complex world.

Successful learners:

- Demonstrate a secure and sophisticated understanding of advanced mathematical concepts and techniques.
- Apply mathematical knowledge confidently to complex and unfamiliar problems.
- Construct rigorous mathematical arguments and proofs.
- Make connections between different branches of mathematics and recognise underlying structures.
- Select and use appropriate mathematical methods efficiently and accurately.
- Communicate mathematical reasoning clearly using precise notation and language.
- Show intellectual curiosity, independence, and resilience in tackling challenging work.
- Achieve outcomes that enable progression to competitive university courses, apprenticeships, and careers.
- Develop confidence in using mathematics as a tool for investigation, modelling, and decision-making.

Ultimately, success in A Level Further Mathematics is characterised by learners becoming independent, highly skilled mathematicians who are prepared to excel in higher education and in careers that require advanced quantitative and analytical expertise.

## 2. Foundational Knowledge

| Area                                | Essential Knowledge / Skills                                                                                                            | Why It Matters                                                                                                                                             |
|-------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Advanced Algebra                    | Complex algebraic manipulation, partial fractions, proof techniques, polynomial functions, inequalities, and advanced equation solving. | Provides the foundation for higher-level mathematics and supports the development of rigorous analytical thinking required in university study.            |
| Proof and Mathematical Reasoning    | Direct proof, proof by contradiction, proof by induction, logical argument, and justification.                                          | Develops the ability to construct and communicate rigorous mathematical arguments, a key skill in mathematics, computer science, and research disciplines. |
| Matrices and Linear Transformations | Matrix operations, inverses, determinants, transformations, and systems of equations.                                                   | Fundamental to engineering, computer graphics, artificial intelligence, data science, and advanced mathematical modelling.                                 |
| Complex Numbers                     | Algebraic and geometric representations, Argand diagrams, modulus and argument, roots of complex numbers.                               | Extends understanding of number systems and underpins applications in physics, engineering, signal processing, and higher mathematics.                     |
| Further Calculus                    | Advanced differentiation and integration techniques, differential equations, hyperbolic functions, and parametric equations.            | Provides essential tools for modelling change and dynamic systems in science, engineering, economics, and research.                                        |
| Vectors                             | Vector algebra, scalar products, vector equations of lines and planes, geometric applications.                                          | Supports spatial reasoning and is widely used in physics, engineering, computer science, and advanced geometry.                                            |
| Polar Coordinates                   | Representing and analysing curves using polar equations and coordinate systems.                                                         | Introduces alternative mathematical representations used in advanced mathematics, physics, and engineering.                                                |
| Differential Equations              | Formulating and solving first-order and second-order differential equations.                                                            | Enables learners to model real-world systems involving growth, decay, motion, and change across scientific disciplines.                                    |
| Further Pure Mathematics            | Advanced functions, series expansions, recurrence relations, and abstract mathematical structures.                                      | Deepens conceptual understanding and prepares learners for undergraduate mathematics and related disciplines.                                              |

|                                        |                                                                                                      |                                                                                                                            |
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| Mechanics (Further)                    | Momentum, collisions, work, energy, power, circular motion, and advanced dynamics.                   | Develops mathematical modelling of physical systems and supports progression to engineering and physics-related courses.   |
| Statistics (Further)                   | Advanced probability distributions, statistical inference, discrete and continuous random variables. | Equips learners with sophisticated data analysis techniques required in finance, economics, research, and data science.    |
| Mathematical Modelling                 | Applying advanced mathematics to represent and solve complex real-world problems.                    | Demonstrates how mathematics is used in industry, technology, science, and decision-making environments.                   |
| Problem Solving in Unfamiliar Contexts | Selecting appropriate methods, connecting different areas of mathematics, and evaluating solutions.  | Encourages flexibility, creativity, and independence, qualities highly valued by universities and employers.               |
| Mathematical Communication             | Using precise notation, formal mathematical language, and structured reasoning.                      | Enables learners to present sophisticated mathematical ideas clearly and accurately in academic and professional settings. |

### 3. Powerful Knowledge

| Powerful Knowledge Area                                   | Why It Matters                                                                                                                                         | Evidence of Understanding                                                                                              |
|-----------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------|
| Proof Establishes Mathematical Truth                      | Mathematics advances through rigorous proof rather than observation alone. Understanding proof develops precision, logic, and intellectual discipline. | Learners construct proofs using contradiction, induction, and direct reasoning, justifying conclusions rigorously.     |
| Complex Numbers Extend Mathematical Possibilities         | Extending beyond the real number system allows solutions to previously unsolvable problems and underpins many modern technologies.                     | Learners manipulate complex numbers algebraically and geometrically, applying them to solve advanced equations.        |
| Mathematical Structures Reveal Hidden Connections         | Advanced mathematics identifies common structures that unite apparently different concepts.                                                            | Learners recognise links between algebra, geometry, calculus, vectors, and matrices, applying knowledge across topics. |
| Abstraction Enables Generalisation                        | Mathematical abstraction allows broad principles to be applied to many different situations.                                                           | Learners formulate general results, identify patterns, and apply abstract concepts in unfamiliar contexts.             |
| Matrices Transform and Model Systems                      | Matrices provide powerful methods for representing transformations and solving complex systems efficiently.                                            | Learners use matrices to solve problems involving transformations, simultaneous equations, and modelling.              |
| Calculus Models Dynamic Systems                           | Advanced calculus provides tools for understanding continuous change, growth, motion, and optimisation.                                                | Learners apply differential and integral techniques to analyse and model complex situations.                           |
| Differential Equations Describe the Real World            | Many natural and engineered systems can be modelled using differential equations.                                                                      | Learners formulate and solve differential equations and interpret solutions within context.                            |
| Vectors Provide a Universal Language for Space and Motion | Vectors allow precise mathematical description of position, direction, and movement in multiple dimensions.                                            | Learners apply vector methods to solve geometric and physical problems accurately.                                     |
| Algorithms Can Optimise Decision-Making                   | Mathematical procedures can identify efficient solutions to complex real-world problems.                                                               | Learners apply graph theory, algorithms, and optimisation techniques to solve decision-based problems.                 |
| Probability Models Uncertainty Systematically             | Advanced probability enables informed decision-making in situations involving risk and uncertainty.                                                    | Learners analyse probability distributions, calculate expected outcomes, and evaluate risk mathematically.             |
| Mathematical Models Have Assumptions and Limitations      | Every model simplifies reality and requires critical evaluation.                                                                                       | Learners assess the validity, strengths, and limitations of mathematical models and assumptions.                       |

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| Multiple Mathematical Representations Enhance Insight    | Different representations reveal different aspects of mathematical relationships.                          | Learners move fluently between algebraic, graphical, numerical, geometric, and matrix representations.     |
| Advanced Mathematics Drives Innovation                   | Many technological, scientific, and economic advances depend on sophisticated mathematical ideas.          | Learners explain how mathematical concepts apply to real-world systems, technologies, and research.        |
| Mathematical Thinking Develops Intellectual Independence | Further Mathematics encourages learners to tackle challenging problems without relying on routine methods. | Learners select appropriate strategies independently, adapt approaches, and evaluate solutions critically. |
| Generalisation and Elegance Are Central to Mathematics   | Mathematicians seek efficient, elegant solutions that explain broad classes of problems.                   | Learners derive general formulae, identify efficient methods, and justify why solutions work.              |

#### 4. Curriculum Implementation

| Term             | Unit                       | Key Content                                                                      | Foundational Knowledge                                      | Powerful Knowledge                                                          | Assessment Opportunities                                         |
|------------------|----------------------------|----------------------------------------------------------------------------------|-------------------------------------------------------------|-----------------------------------------------------------------------------|------------------------------------------------------------------|
| Yr 12 - Autumn 1 | Proof and Advanced Algebra | Proof by contradiction, proof by induction, algebraic methods, complex equations | Algebraic fluency, logical reasoning, mathematical notation | Mathematical truth is established through rigorous proof                    | Baseline assessment, proof tasks, topic tests, retrieval quizzes |
| Yr 12 - Autumn 2 | Complex Numbers            | Imaginary and complex numbers, Argand diagrams, modulus and argument             | Number systems, algebraic manipulation                      | Extending number systems allows solutions to previously unsolvable problems | End-of-unit assessment, exam-style questions                     |

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|------------------|------------------------------|-------------------------------------------------------------------|------------------------------------------------------|--------------------------------------------------------------------------------|---------------------------------------------------|
| Yr 12 - Spring 1 | Matrices and Transformations | Matrix operations, inverses, determinants, linear transformations | Algebraic methods, coordinate geometry               | Matrices provide powerful methods for representing transformations and systems | Topic tests, modelling activities                 |
| Yr 12 - Spring 2 | Further Calculus             | Advanced differentiation and integration techniques               | Calculus from A Level Mathematics, algebraic fluency | Calculus provides a framework for modelling complex change and behaviour       | Formal assessment, problem-solving investigations |
| Yr 12 - Summer 1 | Vectors and Geometry         | Vector algebra, scalar products, equations of lines and planes    | Coordinate geometry, algebraic reasoning             | Vectors provide a universal language for space and motion                      | End-of-unit test, geometric modelling tasks       |
| Yr 12 - Summer 2 | Differential Equations       | First-order differential equations and applications               | Differentiation and integration                      | Mathematical models can describe dynamic real-world systems                    | End-of-year examination, synoptic assessment      |

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|------------------|------------------------------------------------|------------------------------------------------------------------------|-----------------------------------------------------|---------------------------------------------------------------------------------|------------------------------------------------------------------------|
| Yr 13 - Autumn 1 | Polar Coordinates and Further Pure Mathematics | Polar equations, series expansions, recurrence relations               | Coordinate systems, functions, sequences            | Alternative mathematical representations reveal deeper insights                 | Topic tests, extended problem-solving tasks                            |
| Yr 13 - Autumn 2 | Advanced Further Pure Mathematics              | Hyperbolic functions, advanced algebraic structures, advanced calculus | Calculus, algebra, proof                            | Abstraction enables mathematical generalisation across contexts                 | Formal assessment, proof-based investigations                          |
| Yr 13 - Spring 1 | Further Statistics                             | Advanced probability distributions, statistical inference              | Probability and statistics from A Level Mathematics | Statistical models allow informed decision-making under uncertainty             | Statistical investigations, examination questions                      |
| Yr 13 - Spring 2 | Further Mechanics                              | Momentum, collisions, circular motion, work, energy and power          | Mechanics and calculus                              | Mathematics explains and predicts physical systems with precision               | Mechanics assessment, modelling tasks                                  |
| Yr 13 - Summer 1 | Synoptic Further Mathematics                   | Integrated Further Pure, Statistics, Mechanics and                     | Connections across all curriculum content           | Advanced mathematics is interconnected through common structures and principles | Mock examinations, full examination papers, final revision assessments |

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|  |  | Decision Mathematics |  |  |  |
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## 5. Assessment Strategy

| Assessment Type | Purpose                                                                                                                                                                                              | Frequency                                                                                                          |
|-----------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------|
| Diagnostic      | Identify learners' starting points, prior attainment in GCSE and A Level Mathematics content, and readiness for advanced mathematical study. Informs curriculum planning, intervention, and support. | At the start of Year 12, before major new topics, and following intervention programmes where appropriate.         |
| Formative       | Monitor understanding of complex concepts, identify misconceptions, provide feedback, and adapt teaching. Encourages reflection, resilience, and mathematical reasoning.                             | Daily through questioning, retrieval practice, mini-assessments, problem-solving activities, and homework.         |
| Summative       | Measure attainment against curriculum expectations and A Level Further Mathematics standards. Track progress and inform intervention.                                                                | Half-termly/termly formal assessments using examination-style questions and papers.                                |
| Synoptic        | Assess learners' ability to connect knowledge across Further Pure Mathematics, Mechanics and Statistics. Encourages transfer and application of knowledge.                                           | Annually at the end of Year 12. Typically one mock examination series in Autumn Year 13 and one in Spring Year 13. |